

V.P. AND R.P.T.P. SCIENCE COLLEGE , V.V.NAGAR
B.Sc.(MATHEMATICS) SEMESTER - 5
Multiple Choice Question Of US05CMTH21
(Real Analysis)

Unit-1

Que. Fill in the following blanks.

- (1) is not order - complete .
 (a) \mathbb{Q} (b) \mathbb{N} (c) \mathbb{R} (d) \mathbb{C}

- (2) is order - complete .
 (a) \mathbb{Q} (b) \mathbb{N} (c) \mathbb{Z} (d) set of irrational numbers

- (3) is not bounded .
 (a) $\{1, 3, 5, 7, 9\}$ (b) $\{-1, -1/2, -1/3, -1/4, \dots\}$ (c) \mathbb{N} (d) (a, b)

- (4) is ordered field .
 (a) \mathbb{N} (b) \mathbb{Z} (c) set of irrational numbers (d) \mathbb{Q}

- (5) is ordered field .
 (a) \mathbb{R} (b) \mathbb{N} (c) \mathbb{Z} (d) set of irrational numbers

- (6) is not field .
 (a) \mathbb{Q} (b) \mathbb{N} (c) \mathbb{R} (d) \mathbb{C}

- (7) is not field .
 (a) \mathbb{Q} (c) \mathbb{R} (d) I (d) \mathbb{C}

- (8) is complete ordered field .
 (a) \mathbb{Q} (b) \mathbb{N} (c) \mathbb{Z} (d) \mathbb{R}

- (9) Every finite set of numbers is
 (a) bounded (b) field (c) closed (d) open

- (10) $|x|$ $-x$
 (a) \geq (b) \leq (c) $<$ (d) $>$

- (11) $|x - y|$ $|x| + |y|$
 (a) \geq (b) \leq (c) $<$ (d) $>$

- (12) $|x - y|$ $|y - x|$
 (a) \leq (b) $<$ (c) $=$ (d) $>$

- (13) Supremum of set $\left\{1, -1, 1\frac{1}{2}, -1\frac{1}{2}, 1\frac{1}{3}, -1\frac{1}{3}, \dots\right\}$ is
 (a) 1 (b) $1/2$ (c) none of these (d) $1\frac{1}{2}$

- (14) Infimum of set $\left\{1, -1, 1\frac{1}{2}, -1\frac{1}{2}, 1\frac{1}{3}, -1\frac{1}{3}, \dots\right\}$ is
 (a) $-1\frac{1}{2}$ (b) -1 (c) $-1/2$ (d) none of these

- (15) Property of completeness is possess by
- (a) \mathbb{R} (b) \mathbb{Q} (c) \mathbb{N} (d) \mathbb{Z}
- (16) Property of completeness is not possess by
- (a) \mathbb{R} (b) \mathbb{Q} (c) \mathbb{C} (d) none of these
- (17) If a set is bounded above then it hasupper bounds .
- (a) finitely many (b) infinitely many (c) unique (d) two
- (18) If a set is bounded below then it haslower bounds .
- (a) finitely many (b) infinitely many (c) unique (d) two
- (19) There are irrational number between two rational numbers .
- (a) only one (b) infinitely many (c) finitely many (d) at most one
- (20) There are rational numbers between two rational numbers .
- (a) finitely many (b) at most one (c) only one (d) infinitely many
- (21) There are rational numbers between two irrational numbers .
- (a) finitely many (b) at most one (c) only one (d) infinitely many
- (22) The set \mathbb{R} is called continuum .
- (a) geometrical (b) arithmetical (c) universal (d) logical
- (23) The set of points on a line is called continuum .
- (a) geometrical (b) arithmetical (c) universal (d) logical
- (24) Supremum of set $\left\{-\frac{n+1}{n} / n \in \mathbb{N}\right\}$ is
- (a) 1 (b) $1/2$ (c) -1 (d) $1\frac{1}{2}$
- (25) Infimum of set $\left\{-\frac{n+1}{n} / n \in \mathbb{N}\right\}$ is
- (a) -3 (b) -2 (c) -1 (d) $-\frac{1}{2}$
- (26) Infimum of set $\left\{\frac{(-1)^n}{n} / n \in \mathbb{N}\right\}$ is
- (a) -1 (b) -2 (c) 1 (d) $-\frac{1}{2}$
- (27) Supremum of set $\left\{\frac{(-1)^n}{n} / n \in \mathbb{N}\right\}$ is
- (a) -1 (b) -2 (c) 1 (d) $\frac{1}{2}$
- (28) Supremum of set $\left\{1 + \frac{(-1)^n}{n} / n \in \mathbb{N}\right\}$ is
- (a) 1 (b) 2 (c) 3 (d) $\frac{3}{2}$
- (29) Infimum of set $\left\{1 + \frac{(-1)^n}{n} / n \in \mathbb{N}\right\}$ is
- (a) -1 (b) 0 (c) 1 (d) $-\frac{1}{2}$

(30) Greatest element of set $\left\{ 1 + \frac{(-1)^n}{n} / n \in \mathbb{N} \right\}$ is

- (a) 1 (b) 2 (c) 3 (d) $\frac{3}{2}$

(31) Supremum of set $\left\{ \frac{n+1}{n} / n \in \mathbb{N} \right\}$ is

- (a) 1 (b) $\frac{1}{2}$ (c) 2 (d) $1\frac{1}{2}$

(32) Supremum of set $\left\{ \frac{(n+1)^n}{2^n} / n \in \mathbb{N} \right\}$ is

- (a) 9 (b) $\frac{9}{2}$ (c) $\frac{9}{4}$ (d) 0

(33) Infimum of set $\left\{ \frac{(n+1)^n}{2^n} / n \in \mathbb{N} \right\}$ is

- (a) 1 (b) $\frac{9}{2}$ (c) $\frac{9}{4}$ (d) 0

(34) Supremum of set $\left\{ \frac{m}{n} / m, n \in \mathbb{N}, m < 2n \right\}$ is

- (a) 2 (b) $\frac{4}{3}$ (c) 1 (d) 0

(35) Infimum of set $\left\{ \frac{m}{n} / m, n \in \mathbb{N}, m < 2n \right\}$ is

- (a) 2 (b) 0 (c) 1 (d) -1

(36) Supremum of set $\{\sqrt{n} - [\sqrt{n}] / n \in \mathbb{N}\}$ is

- (a) 2 (b) 4 (c) 1 (d) 0

(37) Infimum of set $\{\sqrt{n} - [\sqrt{n}] / n \in \mathbb{N}\}$ is

- (a) 2 (b) 4 (c) 1 (d) 0

(38) Infimum of set $\{x + x^{-1} / x \in \mathbb{R}, x > 0\}$ is

- (a) 2 (b) -2 (c) 1 (d) 0

(39) Infimum of set $\{2^x + 2^{1/x} / x \in \mathbb{R}, x > 0\}$ is

- (a) 2 (b) 0 (c) 1 (d) 4

(40) Supremum of set $\left\{ \frac{m}{m+n} / m, n \in \mathbb{N} \right\}$ is

- (a) 2 (b) $\frac{1}{2}$ (c) 1 (d) 0

(41) Infimum of set $\left\{ \frac{m}{m+n} / m, n \in \mathbb{N} \right\}$ is

- (a) 2 (b) $\frac{1}{2}$ (c) 1 (d) 0

(42) Supremum of set $\left\{ \frac{m}{|m|+n} / m \in \mathbb{Z}, n \in \mathbb{N} \right\}$ is

- (a) 2 (b) $\frac{1}{2}$ (c) 1 (d) 0

(43) Infimum of set $\left\{ \frac{m}{|m|+n} / m \in \mathbb{Z}, n \in \mathbb{N} \right\}$ is

- (a) 1 (b) -1 (c) -2 (d) 0

(44) Supremum of set $\left\{ \frac{(n+m)^2}{2^{mn}} / m, n \in \mathbb{N} \right\}$ is

- (a) 2 (b) 4 (c) 1 (d) 0

(45) Infimum of set $\left\{ \frac{(n+m)^2}{2^{mn}} / m, n \in \mathbb{N} \right\}$ is

- (a) 2 (b) 4 (c) 1 (d) 0

(46) Infimum of set $\left\{ \frac{m}{n} + \frac{4n}{m} / m, n \in \mathbb{N} \right\}$ is

- (a) 2 (b) 4 (c) 1 (d) 0

(47) Infimum of set $\left\{ \frac{mn}{4m^2+n^2} / m, n \in \mathbb{N} \right\}$ is

- (a) 1 (b) 1/4 (c) 1/2 (d) 0

(48) Infimum of set $\left\{ m + \frac{1}{n} / m, n \in \mathbb{N} \right\}$ is

- (a) 2 (b) 1 (c) -1 (d) 0

(49) Infimum of set $\left\{ \pi + \frac{1}{2^n} / n \in \mathbb{N} \right\}$ is

- (a) 1 (b) π (c) $\pi+1$ (d) 0

(50) Supremum of set $\left\{ \pi + \frac{1}{2^n} / n \in \mathbb{N} \right\}$ is

- (a) 1 (b) π (c) $\pi + \frac{1}{2}$ (d) 0

(51) Supremum of set $\left\{ \sin\left(\frac{n\pi}{6}\right) / n \in \mathbb{N} \right\}$ is

- (a) 1 (b) -1 (c) 2 (d) 0

(52) Infimum of set $\left\{ \sin\left(\frac{n\pi}{6}\right) / n \in \mathbb{N} \right\}$ is

- (a) 1 (b) -1 (c) 1/2 (d) 0

(53) Supremum of set $\{-2 \sin x / x \in \mathbb{R}\}$ is

- (a) 1 (b) -1 (c) 2 (d) 0

(54) Infimum of set $\{-2 \sin x / x \in \mathbb{R}\}$ is

- (a) 1 (b) -1 (c) 2 (d) -2

(55) Infimum of set $\left\{ \frac{n+1}{n} / n \in \mathbb{N} \right\}$ is

- (a) -1 (b) 1/2 (c) 1 (d) 0

(56) Infimum of set $\left\{ \frac{n}{n+1} / n \in \mathbb{N} \right\}$ is

- (a) 1/3 (b) 1 (c) 1/2 (d) 0

(57) Supremum of set $\left\{ \frac{n}{n+1} / n \in \mathbb{N} \right\}$ is

- (a) 2 (b) 1 (c) 1/2 (d) 0

(58) Supremum of set $\{0.2, 0.22, 0.222, \dots\}$ is

- (a) 2 (b) 0.23 (c) 0.3 (d) 0

(59) Infimum of set $\{0.2, 0.22, 0.222, \dots\}$ is

- (a) 0.2 (b) 0.22 (c) 0.21 (d) 0

- (60) Supremum of set $\left\{ (-1)^n \left(\frac{1}{4} - \frac{4}{n} \right) / n \in \mathbb{N} \right\}$ is
 (a) 4 (b) $15/4$ (c) $1/4$ (d) 1
- (61) Infimum of set $\left\{ (-1)^n \left(\frac{1}{4} - \frac{4}{n} \right) / n \in \mathbb{N} \right\}$ is
 (a) $-7/4$ (b) $-1/4$ (c) $-9/4$ (d) -1
- (62) Number of limit point of the set $\left\{ \frac{1}{m} + \frac{1}{n} / m, n \in \mathbb{N} \right\}$ is/are
 (a) 1 (b) 2 (c) finitely many (d) infinitely many
- (63) The limit point of the set $\left\{ \frac{1}{n} \sin \frac{1}{n} / n \in \mathbb{N} \right\}$ is
 (a) 1 (b) 0 (c) finitely many (d) infinitely many
- ## UNIT-2
- (1) Interior point of \mathbb{N} is
 (a) 1 (b) ϕ (c) \mathbb{N} (d) none of these
- (2) Interior point of \mathbb{Q} is
 (a) 1 (b) ϕ (c) \mathbb{Q} (d) \mathbb{R}
- (3) Interior point of \mathbb{R} is
 (a) 1 (b) ϕ (c) \mathbb{Q} (d) \mathbb{R}
- (4) $S^i = S$
 (a) \subseteq (b) \supset (c) \leq (d) \subset
- (5) If S is open set then $S^i = S$
 (a) \leq (b) \supset (c) $=$ (d) \subset
- (6) If $S_n = (-1/n, 1/n)$, $n \in \mathbb{N}$ then $\cap S_n =$
 (a) ϕ (b) 1 (c) $\{0\}$ (d) 0
- (7) $I' =$
 (a) ϕ (b) I (c) $\{0\}$ (d) \mathbb{R}
- (8) $\mathbb{Q}' =$
 (a) ϕ (b) \mathbb{R} (c) $\{0\}$ (d) \mathbb{Q}
- (9) $\mathbb{R}' =$
 (a) ϕ (b) \mathbb{R} (c) $\{0\}$ (d) \mathbb{Q}
- (10) Every finite set has limit point.
 (a) 1 (b) $\{0\}$ (c) no (d) finite
- (11) $S' \cap T' = (S \cap T)'$.
 (a) $=$ (b) \supset (c) \leq (d) \subset
- (12) $\tilde{S} = S = S'$.
 (a) δ (b) $+$ (c) \cap (d) \cup

- (13) $\tilde{I} = \dots$
 (a) ϕ (b) I (c) \mathbb{Q} (d) \mathbb{R}
- (14) $\tilde{\phi} = \dots$
 (a) ϕ (b) I (c) \mathbb{Q} (d) \mathbb{R}
- (15) $\tilde{\mathbb{Q}} = \dots$
 (a) ϕ (b) I (c) \mathbb{Q} (d) \mathbb{R}
- (16) $\tilde{\mathbb{R}} = \dots$
 (a) ϕ (b) I (c) \mathbb{Q} (d) \mathbb{R}
- (17) $\left\{1, -1, 1\frac{1}{2}, -1\frac{1}{2}, 1\frac{1}{3}, -1\frac{1}{3}, \dots\right\}$ is
 (a) open and closed (b) open but not closed (c) closed but not open (d) none
- (18) If $S_n = [1 + 1/n, 3]$, $n \in \mathbb{N}$ then $\cup S_n = \dots$
 (a) $[1, 3]$ (b) $[1, 3)$ (c) ϕ (d) $(1, 3]$
- (19) Limit point of set $\left\{1, -1, 1\frac{1}{2}, -1\frac{1}{2}, 1\frac{1}{3}, -1\frac{1}{3}, \dots\right\}$ are
 (a) $1, -1$ (b) only 1 (c) only -1 (d) none of these
- (20) If $S = \left\{1, -1, 1\frac{1}{2}, -1\frac{1}{2}, 1\frac{1}{3}, -1\frac{1}{3}, \dots\right\}$ then $\inf S' = \dots$
 (a) $1\frac{1}{2}$ (b) -1 (c) 1 (d) $-1\frac{1}{2}$
- (21) If $S = \left\{1, -1, 1\frac{1}{2}, -1\frac{1}{2}, 1\frac{1}{3}, -1\frac{1}{3}, \dots\right\}$ then $\sup S' = \dots$
 (a) $-1\frac{1}{2}$ (b) -1 (c) 1 (d) $1\frac{1}{2}$
- (22) If $S = \left\{1, -1, 1\frac{1}{2}, -1\frac{1}{2}, 1\frac{1}{3}, -1\frac{1}{3}, \dots\right\}$ then $\sup \tilde{S} = \dots$
 (a) $-1\frac{1}{2}$ (b) -1 (c) $1\frac{1}{2}$ (d) 1
- (23) If $S = \left\{1, -1, 1\frac{1}{2}, -1\frac{1}{2}, 1\frac{1}{3}, -1\frac{1}{3}, \dots\right\}$ then $\inf \tilde{S} = \dots$
 (a) $-1\frac{1}{2}$ (b) 1 (c) $1\frac{1}{2}$ (d) -1
- (24) Set S is closed iff
 (a) $S' \subset S$ (b) $S' \supset S$ (c) $S' \neq S$ (d) $S' = S$
- (25) If M is supremum of S and $M \notin S$ then M is of S .
 (a) closure (b) limit point (c) derived set (d) identity
- (26) If M is supremum of S and $M \notin S$ then M is greatest member of
 (a) S (b) \tilde{S} (c) S' (d) \mathbb{R}
- (27) $\bigcup_{n \in \mathbb{N}} \left[a + \frac{1}{n}, a + 2 \right], a \in \mathbb{R}$ is set.
 (a) closed (b) open (c) universal (d) not closed

- (28) The set of limit points of the set $[0, 1] - \left\{ \frac{1}{n} / n \in \mathbb{N} \right\}$ is
 (a) countable (b) uncountable (c) finite (d) empty
- (29) Limit point of the set $\left\{ \frac{1}{n} \sin \frac{1}{n} / n \in \mathbb{N} \right\}$ is
 (a) 1 (b) 0 (c) -1 (d) 0,1
- (30) The set of limit points of the set $\left\{ \frac{2}{x+1} / x \in (-1, 1) \right\}$ is
 (a) $[1, \infty)$ (b) $(1, \infty)$ (c) $[-1, 1]$ (d) $[-1, \infty)$
- (31) The set of limit points of the set $\left\{ \frac{5-x}{x} / x \in (2, 3) \right\}$ is
 (a) $[2/3, 3/2)$ (b) $(2/3, 3/2)$ (c) $[2/3, 3/2]$ (d) $[2/3, \infty)$
- (32) The set of limit points of the set $\left\{ \frac{5-x}{3} / x \in (2, 3) \right\}$ is
 (a) $[2/3, 1)$ (b) $(2/3, 1)$ (c) $[2/3, 1]$ (d) $[2/3, \infty)$
- (33) Derived set of the set $\{x / 0 < x < 1, x \in \mathbb{Q}\}$ is
 (a) $[0, 1)$ (b) $(0, 1)$ (c) $[0, 1]$ (d) $(0, 1]$
- (34) Derived set of the set $\left\{ \frac{1}{m} + \frac{1}{n} / m, n \in \mathbb{N} \right\}$ is
 (a) $\left\{ \frac{1}{m} / m \in \mathbb{N} \right\} \cup \{0\}$ (b) $\left\{ \frac{1}{m} / m \in \mathbb{N} \right\}$ (c) $\{0\}$ (d) $(0, 1]$
- (35) Derived set of the set $\left\{ 1 + \frac{1}{2^n} / n \in \mathbb{N} \right\}$ is
 (a) $\{0\}$ (b) $\{1\}$ (c) $[0, 1]$ (d) $(0, 1]$
- (36) Derived set of the set $\left\{ 3^{-n} + 5^{-n} / n \in \mathbb{N} \right\}$ is
 (a) $\{0\}$ (b) $\{1\}$ (c) $\{3^{-1}\}$ (d) 0
- (37) Derived set of the set $\left\{ \frac{1}{n} / n \in \mathbb{Z}, n \neq 0 \right\}$ is
 (a) $\{0, 1\}$ (b) $\{-1, 1\}$ (c) $\{-1\}$ (d) $\{0\}$
- (38) Derived set of the set $\left\{ 1 + \frac{(-1)^n}{n} / n \in \mathbb{N} \right\}$ is
 (a) $\{0\}$ (b) $\{1\}$ (c) $[0, 1]$ (d) 1
- (39) Derived set of the set $\left\{ \frac{1 + (-1)^n}{n} / n \in \mathbb{N} \right\}$ is
 (a) $\{0\}$ (b) $\{1\}$ (c) $[0, 1]$ (d) 0
- (40) Derived set of the set $\left\{ (-1)^n + \frac{1}{n} / n \in \mathbb{N} \right\}$ is
 (a) $\{-1\}$ (b) $\{1\}$ (c) $\{-1, 1\}$ (d) $-1, 1$
- (41) Derived set of the set $\left\{ \frac{1}{2m} + \frac{1}{3n} / m, n \in \mathbb{N} \right\}$ is
 (a) $\left\{ \frac{1}{2m} / m \in \mathbb{N} \right\} \cup \{0\}$ (b) $\left\{ \frac{1}{3n} / m \in \mathbb{N} \right\}$ (c) $\{0\}$ (d) $\left\{ \frac{1}{2m} / m \in \mathbb{N} \right\} \cup \left\{ \frac{1}{3n} / n \in \mathbb{N} \right\}$
- (42) Derived set of the set $\left\{ \frac{n}{n+1} / n \in \mathbb{N} \right\}$ is
 (a) $\{0, 1\}$ (b) $\{1\}$ (c) $\{-1\}$ (d) $\{0\}$
- (43) Derived set of the set $\left\{ m + \frac{1}{n} / m, n \in \mathbb{N} \right\}$ is
 (a) $\{0\}$ (b) \mathbb{N} (c) $[0, 1]$ (d) \emptyset

- (44) Derived set of the set $\left\{ n + \frac{1}{n} / n \in \mathbb{N} \right\}$ is
 (a) $\{0\}$ (b) \mathbb{N} (c) $[0, 1]$ (d) \emptyset
- (45) Derived set of the set $(2, 3) \cup \left\{ 4 + \frac{1}{n} / n \in \mathbb{N} \right\} \cup \{5\}$ is
 (a) \emptyset (b) $(2, 4) \cup \{5\}$ (c) $[2, 5]$ (d) $[2, 3] \cup \{4\}$
- (46) $(\mathbb{Q}^c)' = \dots$
 (a) ϕ (b) \mathbb{R} (c) $\{0\}$ (d) \mathbb{Q}
- (47) If $S = \left\{ \frac{1}{n} / n \in \mathbb{N} \right\}$ then $\bar{S} = \dots$
 (a) ϕ (b) $S \cup \{0\}$ (c) $\{0\}$ (d) S
- (48) If $S = \left\{ 1 - \frac{2}{n} / n \in \mathbb{N} \right\}$ then $\bar{S} = \dots$
 (a) ϕ (b) $S \cup \{0\}$ (c) $\{0\}$ (d) $S \cup \{1\}$
- (49) If $S = \mathbb{R} - \left\{ \frac{1}{n} / n \in \mathbb{N} \right\}$ then $\bar{S} = \dots$
 (a) \mathbb{R} (b) $S \cup \{0\}$ (c) $\{0\}$ (d) $S \cup \{1\}$
- (50) If $S = \left\{ \frac{1}{m} + \frac{1}{n} / m, n \in \mathbb{N} \right\}$ then $\bar{S} = \dots$
 (a) $\left\{ \frac{1}{n} / n \in \mathbb{N} \right\} \cup \left\{ \frac{1}{m} + \frac{1}{n} / m, n \in \mathbb{N} \right\} \cup \{0\}$ (b) $\left\{ \frac{1}{m} / m \in \mathbb{N} \right\}$ (c) $\{0\}$ (d) $\left\{ \frac{1}{n} / n \in \mathbb{N} \right\} \cup \{0\}$
- (51) Closure of $\mathbb{R} - \mathbb{N}$ is
 (a) $\{0\}$ (b) \mathbb{N} (c) \mathbb{R} (d) \emptyset
- (52) Closure of $\mathbb{R} - \mathbb{Z}$ is
 (a) $\{0\}$ (b) \mathbb{Z} (c) \mathbb{R} (d) \emptyset
- (53) Closure of $\mathbb{R} - \mathbb{Q}$ is
 (a) $\{0\}$ (b) \mathbb{Q} (c) \mathbb{R} (d) \emptyset
- (54) Closure of $\mathbb{R} - \mathbb{Q}^c$ is
 (a) $\{0\}$ (b) \mathbb{Q}^c (c) \mathbb{R} (d) \emptyset

UNIT-3

- (1) If $S_n = 1 + (-1)^n$, $n \in \mathbb{N}$ then limit points of sequence $\{S_n\}$ are
 (a) $0, 2$ (b) $1, 2$ (c) $-1, 1$ (d) none of these
- (2) If $S_n = (-1)^n$, $n \in \mathbb{N}$ then limit points of sequence $\{S_n\}$ are
 (a) $0, 2$ (b) $1, 2$ (c) $-1, 1$ (d) none of these
- (3) If $S_n = (-1)^n \left(1 + \frac{1}{n} \right)$, $n \in \mathbb{N}$ then limit points of sequence $\{S_n\}$ are
 (a) $0, 2$ (b) $1, 2$ (c) $-1, 1$ (d) none of these
- (4) If $S_n = 1 + (-1)^n$, $n \in \mathbb{N}$ then the range set of sequence $\{S_n\}$ has limit point .
 (a) $0, 2$ (b) $1, 2$ (c) $-1, 1$ (d) no
- (5) If $S_n = (-1)^n$, $n \in \mathbb{N}$ then the range set of sequence $\{S_n\}$ has limit point .
 (a) $0, 2$ (b) $1, 2$ (c) $-1, 1$ (d) no

- (6) Lower limit of sequence $\{(-1)^n\}$ is
 (a) 0 (b) 1 (c) -1 (d) none of these
- (7) Upper limit of sequence $\{1 + (-1)^n\}$ is
 (a) 0 (b) 1 (c) 2 (d) none of these
- (8) Sequence $\{1 + (-1)^n\}$ is
 (a) oscillates finitely (b) diverges to $+\infty$ (c) oscillates infinitely (d) diverges to $-\infty$
- (9) Sequence $\left\{ (-1)^n \left(1 + \frac{1}{n} \right) \right\}$ is
 (a) oscillates finitely (b) diverges to $+\infty$ (c) oscillates infinitely (d) diverges to $-\infty$
- (10) Sequence $\{n(-1)^n\}$ is
 (a) oscillates finitely (b) diverges to $+\infty$ (c) oscillates infinitely (d) diverges to $-\infty$
- (11) Sequence $\{n^2\}$ is
 (a) oscillates finitely (b) diverges to $+\infty$ (c) oscillates infinitely (d) diverges to $-\infty$
- (12) Sequence $\{-2^n\}$ is
 (a) oscillates finitely (b) diverges to $+\infty$ (c) oscillates infinitely (d) diverges to $-\infty$
- (13) Sequence $\{1, 2, 1/2, 3, 1/3, \dots\}$ is
 (a) oscillates finitely (b) diverges to $+\infty$ (c) oscillates infinitely (d) diverges to $-\infty$
- (14) Sequence $\{1, 2, 3, 2, 5, 2, 7, 2, 3, 2, 11, 2, 13, \dots\}$ is
 (a) oscillates finitely (b) diverges to $+\infty$ (c) oscillates infinitely (d) diverges to $-\infty$
- (15) $\lim_{n \rightarrow \infty} n^{1/n} = \dots$
 (a) n (b) ∞ (c) 0 (d) 1
- (16) the sequence $\{r^n\}$ converges iff
 (a) $-1 < r \leq 1$ (b) $-1 < r < 1$ (c) $-1 \leq r \leq 1$ (d) $-1 \leq r < 1$
- (17) The sequence $\{r^n\}$ converges to zero iff
 (a) $|r| \geq 1$ (b) $|r| < 1$ (c) $|r| \leq 1$ (d) $|r| > 1$
- (18) $\lim \frac{1+2+3+\dots+n}{n^2} = \dots$
 (a) $1/n$ (b) 1 (c) 0 (d) $1/2$
- (19) $\lim \frac{1+3+5+\dots+(2n-1)}{n^2} = \dots$
 (a) $1/n$ (b) 1 (c) 0 (d) $1/2$
- (20) $\lim_{n \rightarrow \infty} \left(1 + \frac{1}{n} \right)^n = \dots$
 (a) 1 (b) ∞ (c) 0 (d) e
- (21) A limit point of the sequence a limit point of the range set of a sequence .
 (a) is also (b) is same as (c) need not be (d) none of these
- (22) Every bounded sequence has limit point .
 (a) unique (b) at least one (c) finite (d) infinite

- (23) A bounded sequence with limit point is convergent .
 (a) unique (b) at least one (c) finite (d) infinite
- (24) $\lim_{n \rightarrow \infty} \frac{x^n}{n!} = \dots$
 (a) e (b) ∞ (c) 0 (d) 1
- (25) The limit point of sequence $\left\{ m + \frac{1}{n} \right\}$ are
 (a) $e, 1$ (b) $0, 1$ (c) $1, 2, 3, 4, \dots$ (d) $1, 1/2, 1/3, 1/4, \dots$
- (26) The limit point of sequence $\left\{ \frac{1}{m} + \frac{1}{n} \right\}$ are
 (a) $e, 1$ (b) $0, 1$ (c) $1, 2, 3, 4, \dots$ (d) $1, 1/2, 1/3, 1/4, \dots$
- (27) The sequence $\{(-1)^n\}$ is
 (a) bounded and convergent (b) bounded and divergent (c) unbounded and convergent (d) unbounded and divergent
- (28) The sequence is convergent .
 (a) $\{2^n\}$ (b) $\{(1/3)^n\}$ (c) $\{3^n\}$ (d) none of these
 none of these
- (29) The sequence is divergent .
 (a) $\left\{ 1 + \frac{1}{n} \right\}$ (b) $\left\{ \frac{(-1)^{n-1}}{n!} \right\}$ (c) $\left\{ \frac{(-1)^n}{n^2} \right\}$ (d) $\{(1/3)^n\}$
- (30) The sequence is divergent .
 (a) $\left\{ (-1)^n \left(1 + \frac{1}{n} \right) \right\}$ (b) $\left\{ \frac{(-1)^{n-1}}{n!} \right\}$ (c) $\left\{ \frac{(-1)^n}{n^2} \right\}$ (d) $\{(1/3)^n\}$
- (31) If $L = \lim_{n \rightarrow \infty} \frac{1}{\sqrt[n]{n!}}$ then
 (a) $L = 0$ (b) $L = 1$ (c) $0 < L < 1$ (d) $L = \infty$
- (32) $\lim_{n \rightarrow \infty} \frac{1}{n} \left(1 + \frac{1}{2} + \frac{1}{3} + \frac{1}{4} + \dots \right)$ is
 (a) $\frac{1}{2}$ (b) 1 (c) 0 (d) $1/2$
- (33) $\lim_{n \rightarrow \infty} \left(1 + \frac{x}{n} \right)^n = \dots$
 (a) e^x (b) 1 (c) 0 (d) e
- (34) $\lim_{n \rightarrow \infty} \frac{\log n}{n} = \dots$
 (a) ∞ (b) 1 (c) 0 (d) e
- (35) $\lim_{n \rightarrow \infty} \frac{1}{(n)^n} = \dots$
 (a) e (b) ∞ (c) 0 (d) 1
- (36) $\lim_{n \rightarrow \infty} \left(\frac{1}{n} \right)^{\frac{1}{n}} = \dots$
 (a) e (b) ∞ (c) 0 (d) 1

(37) $\lim_{n \rightarrow \infty} \left(\frac{1}{n^2} \right)^{\frac{1}{n}} = \dots$
 (a) e (b) ∞ (c) 0 (d) 1

(38) The sequence $\left\{ \frac{n}{n+1} \right\}$ is
 (a) decreasing (b) increasing (c) unbounded (d) none of these

(39) The sequence $\left\{ a + \frac{(-1)^n b}{n} \right\}$ is
 (a) bounded (b) unbounded (c) convergent (d) none of these

(40) If $S = \left\{ \frac{1}{n} / n \in \mathbb{N}, n \text{ is prime} \right\}$, $T = \{x^2 / x \in \mathbb{R}\}$ then
 (a) $\sup(S \cap T) = 1$ (b) $\sup S = 1$, $\inf T = 0$ (c) $\sup S = 1/2$, $\inf T = 0$
 (d) $\inf(S \cup T) = 1/2$

(41) For sequence $a_n = \left(1 + (-1)^n \frac{1}{n} \right)^n$, $\limsup a_n = \dots$
 (a) 0 (b) 1 (c) e (d) $1/e$

(42) For sequence $a_n = \left(1 + (-1)^n \frac{1}{n} \right)^n$, $\liminf a_n = \dots$
 (a) 0 (b) 1 (c) e (d) $1/e$

(43) Limit points of the sequence $a_n = \left(1 + (-1)^n \frac{1}{n} \right)^n$ is/are
 (a) 1 (b) only $1/e$ (c) only e (d) e and $1/e$

UNIT-4

(1) The series $\frac{1}{2} + \frac{2}{3} + \frac{3}{4} + \dots$ is
 (a) not convergent (b) oscillating (c) convergent (d) none of these

(2) The series $1 + \frac{1}{2!} + \frac{1}{3!} + \dots$ is
 (a) not convergent (b) oscillating (c) convergent (d) none of these

(3) The series $\frac{1}{(\log 2)^p} + \frac{1}{(\log 3)^p} + \dots + \frac{1}{(\log n)^p} + \dots$ is for $p > 0$.
 (a) oscillating (b) divergent (c) convergent (d) none of these

(4) The series $\frac{1 \cdot 2}{3^2 \cdot 4^2} + \frac{3 \cdot 4}{5^2 \cdot 6^2} + \frac{5 \cdot 6}{7^2 \cdot 8^2} + \dots$ is
 (a) convergent (b) divergence (c) oscillating (d) none of these

(5) The series $\frac{1}{1 \cdot 2 \cdot 3} + \frac{3}{2 \cdot 3 \cdot 4} + \frac{5}{3 \cdot 4 \cdot 5} + \dots$ is
 (a) oscillating (b) convergent (c) not convergent (d) none of these

(6) The series $\frac{1}{\sqrt{1 \cdot 2}} + \frac{1}{\sqrt{2 \cdot 3}} + \frac{1}{\sqrt{3 \cdot 4}} + \dots$ is
 (a) oscillating (b) divergent (c) convergent (d) none of these

(7) The series $\frac{1}{4 \cdot 6} + \frac{\sqrt{3}}{6 \cdot 8} + \frac{\sqrt{5}}{8 \cdot 10} + \frac{\sqrt{7}}{10 \cdot 12} + \dots$ is
 (a) oscillating (b) not convergent (c) convergent (d) none of these

(8) $\sum \frac{n+1}{n^p}$ is convergent for
 (a) $p > 2$ (b) $p < 2$ (c) $p = 1$ (d) $p < 1$

- (9) $\sum \frac{1}{\sqrt{n} + \sqrt{n+1}}$ is
 (a) divergence (b) convergent (c) oscillating (d) none of these
- (10) $\sum \sin \frac{1}{n^2}$ is
 (a) divergence (b) convergent (c) oscillating (d) none of these
- (11) $\sum \cos \frac{1}{n}$ is
 (a) divergence (b) convergent (c) oscillating (d) none of these
- (12) $\sum \frac{1}{\sqrt{n}} \tan \frac{1}{n}$ is
 (a) divergence (b) convergent (c) oscillating (d) none of these
- (13) $\sum \frac{\sqrt{n+1} + \sqrt{n-1}}{n}$ is
 (a) divergence (b) convergent (c) oscillating (d) none of these
- (14) $\frac{x}{1} + \frac{x^2}{2} + \frac{x^3}{3} + \frac{x^4}{4} + \dots$ is convergent for
 (a) $|x| > 1$ (b) $|x| < 1$ (c) $|x| \leq 1$ (d) $|x| \geq 1$
- (15) $\frac{x}{1} + \frac{x^2}{2} + \frac{x^3}{3} + \frac{x^4}{4} + \dots$ is divergent for
 (a) $|x| > 1$ (b) $|x| < 1$ (c) $|x| \geq 1$ (d) $|x| = 1$
- (16) $\frac{x^2}{2\sqrt{1}} + \frac{x^3}{3\sqrt{2}} + \frac{x^4}{4\sqrt{3}} + \frac{x^5}{5\sqrt{4}} + \dots$ is convergent for
 (a) $|x| > 1$ (b) $|x| < 1$ (c) $|x| \leq 1$ (d) $|x| \geq 1$
- (17) $\frac{x^2}{2\sqrt{1}} + \frac{x^3}{3\sqrt{2}} + \frac{x^4}{4\sqrt{3}} + \frac{x^5}{5\sqrt{4}} + \dots$ is divergent for
 (a) $|x| > 1$ (b) $|x| < 1$ (c) $|x| \leq 1$ (d) $|x| \geq 1$
- (18) $1 + \frac{x^2}{2^p} + \frac{x^4}{4^p} + \frac{x^6}{6^p} + \dots$ is divergent for
 (a) $|x| > 1$ (b) $|x| < 1$ (c) $|x| \geq 1$ (d) $|x| \leq 1$
- (19) $1 + \frac{x^2}{2^p} + \frac{x^4}{4^p} + \frac{x^6}{6^p} + \dots$ is convergent for
 (a) $|x| > 1$ (b) $|x| < 1$ (c) $|x| \geq 1$ (d) $|x| \leq 1$
- (20) $1 + \frac{1}{2^p} + \frac{1}{4^p} + \frac{1}{6^p} + \dots$ is divergent for
 (a) $p > 1$ (b) $p < 1$ (c) $p \geq 1$ (d) $p \leq 1$
- (21) $1 + \frac{1}{2^p} + \frac{1}{4^p} + \frac{1}{6^p} + \dots$ is convergent for
 (a) $p > 1$ (b) $p < 1$ (c) $p \geq 1$ (d) $p \leq 1$
- (22) $\frac{1}{2} + \frac{1}{3^2} + \frac{1}{2^3} + \frac{1}{3^4} + \dots$ is
 (a) 0 (b) 1 (c) convergent (d) not convergent
- (23) A positive term series can not
 (a) oscillate (b) divergent to $+\infty$ (c) convergent (d) None of these
- (24) The series $\sum \frac{1}{\left(1 + \frac{1}{n}\right)^{n^2}}$ is
 (a) oscillate (b) divergent (c) convergent (d) None of these

- (25) The series $\sum \frac{\sqrt{n}}{n^2 + 1}$ is
(a) oscillate (b) divergent (c) convergent (d) None of these
- (26) The series $\sum \frac{x^n}{x+n}$ is convergent if
(a) $x < 1$ (b) $x > 1$ (c) $x = 1$ (d) $0 < x < 1$
- (27) The series $1 + \frac{1}{2^2} + \frac{2^2}{3^3} + \frac{3^3}{4^4} + \dots$ is
(a) oscillate (b) divergent (c) convergent (d) None of these
- (28) The series $\sum \frac{n^2}{3^n}$ is
(a) unbounded (b) divergent (c) convergent (d) None of these
- (29) The series $\sum \frac{2n+1}{(n^2+n)^2}$ is convergent to
(a) 1 (b) number > 1 (c) 0 (d) None of these
- (30) $\sqrt[7]{\frac{1}{2}} + \sqrt[7]{\frac{2}{3}} + \sqrt[7]{\frac{3}{4}} + \dots$ is
(a) oscillate (b) divergent (c) convergent (d) None of these
- (31) The series $\sum n \log \left(\frac{3n+2}{3n-2} - 1 \right)$ is
(a) oscillate (b) divergent (c) convergent (d) None of these
- (32) The series $\sum \frac{3^n}{3^n + 4^n}$ is
(a) oscillate (b) divergent (c) convergent (d) None of these
- (33) The series $\sum \frac{5^n}{4^n + 5^n}$ is
(a) oscillate (b) divergent (c) convergent (d) None of these
- NOTE : (i) The series $\sum \frac{a^n}{a^n + b^n}$ is convergent if $0 < \frac{a}{b} < 1$ and is divergent if $\frac{a}{b} > 1$.
(ii) The series $\sum \frac{a}{bn^p \pm c}$, ($b \neq 0$) is convergent if $p > 1$ and is divergent if $p \leq 1$.
- (34) The series $\sum \frac{1}{n^{50} - 500}$ is
(a) oscillate (b) divergent (c) convergent (d) None of these
- (35) The series $\sum \frac{2}{3n^2 - 2^2}$ is
(a) oscillate (b) divergent (c) convergent (d) None of these
- (36) The series $\sum \frac{6}{4n^{48} - 62}$ is
(a) oscillate (b) divergent (c) convergent (d) None of these
- (37) The series $\sum \frac{2}{7\sqrt{n} - 2^3}$ is
(a) oscillate (b) divergent (c) convergent (d) None of these
- (38) The series $\sum \frac{5}{7n + 2^3}$ is
(a) oscillate (b) divergent (c) convergent (d) None of these

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- (39) The series $\sum \frac{100}{2\sqrt[3]{n} + 50}$ is
- (a) oscillate (b) divergent (c) convergent (d) None of these
- (40) The series $\sum \frac{4 \cdot 7 \cdot 10 \dots (3n+1)}{1 \cdot 2 \cdot 3 \dots n} x^n$ is convergent if
- (a) $|x| < \frac{1}{3}$ (b) $|x| < 1$ (c) $|x| < \frac{1}{2}$ (d) $|x| < \frac{1}{4}$